

Solution to Problems

1. All positive real numbers form a group with respect to ordinary multiplication.
2. All complex numbers form a group with respect to ordinary addition.
3. Let a and b be two different group elements such that $a \cdot c = d$ and $b \cdot c = d$. Let us multiply these two equations by c^{-1} from the left: $a = d \cdot c^{-1}$ and $b = d \cdot c^{-1}$. Thus we have then the elements $a = b$ and our initial suppose was incorrect. Therefore, in one line of the multiplication table there cannot be two equal group elements.
4. The symmetry groups of the molecules: H_2O : \mathbf{C}_{2v} , NH_3 : \mathbf{C}_{3v} , CH_4 : \mathbf{T}_d , UF_6 : \mathbf{O}_h .
5. The multiplication table for the point symmetry group \mathbf{C}_4 :

	E	C_4	C_2	C_4^3
E	E	C_4	C_2	C_4^3
C_4	C_4	C_2	C_4^3	E
C_2	C_2	C_4^3	E	C_4
C_4^3	C_4^3	E	C_4	C_2

- 6.
7. Hint: check the corresponding boxes of the multiplication table.
8. hint: check the corresponding boxes of the multiplication table.
9. Hint: from the equations (i) (10) and (ii) (14) get the corresponding relations between parameters.
10. Hint: check that the group postulates are satisfied.
11. Among the elements there is no identity element.
12. $n(n - 1)/2$ parameters.
13. Hint: show that $x'^2 - y'^2 = x^2 - y^2$.